Synchrotron vacuum ultraviolet radiation studies of the $D^{1}Π_u$ state of H$_2$

G. D. Dickenson,$^1$ T. I. Ivanov,$^1$ M. Roudjane$^{2,a}$ N. de Oliveira,$^2$ D. Joyeux,$^{2,3}$ L. Nahon,$^2$ W.-U. L. Tchang-Brillet,$^4$ M. Glass-Maujean,$^5$ I. Haar,$^6$ A. Ehresmann,$^6$ and W. Ubachs$^{1,6,7}$

$^1$Institute for Lasers, Life and Biophotonics Amsterdam, VU University, De Boelelaan 1081, 1081 HV Amsterdam, The Netherlands
$^2$Synchrotron Soleil, Orme des Merlontiers, St. Aunin, BP 48, 91126 Gif sur Yvette Cedex, France
$^3$Laboratoire Charles Fabry de l’Institut d’Optique, CNRS, Université Paris–Sud Campus Polytechnique, RD 128, 91127 Palaiseau Cedex, France
$^4$Laboratoire d’Étude du Rayonnement et de la Matière en Astrophysique, UMR 8112 du CNRS, Observatoire de Paris-Meudon Université UPMC, 5 Place Jules Janssen, 92195 Meudon Cedex, France
$^5$Laboratoire de Physique Moléculaire pour l’Atmosphère et l’Astrophysique, UMR 7092, Université P. et M. Curie, 4 Place Jussieu, 75252 Paris Cedex 05, France
$^6$Institute of Physics and Center for Interdisciplinary Nanostructure Science and Technology, Heinrich Plett Str. 40, 34132 Kassel, Germany

(Received 27 July 2010; accepted 26 September 2010; published online 14 October 2010; corrected xx November 2010)

The $3pπD^{1}Π_u$ state of the H$_2$ molecule was reinvestigated with different techniques at two synchrotron installations. The Fourier transform spectrometer in the vacuum ultraviolet wavelength range of the DESIRS beamline at the SOLEIL synchrotron was used for recording absorption spectra of the $D^{1}Π_u$ state at high resolution and high absolute accuracy, limited only by the Doppler contribution at 100 K. From these measurements, line positions were extracted, in particular, for the narrow resonances involving $1Π_u^-$ states, with an accuracy estimated at 0.06 cm$^{-1}$. The new data also closely match multichannel quantum defect calculations performed for the $Π^-$ components observed via the narrow Q-lines. The $Λ$-doubling in the $D^{1}Π_u$ state was determined up to $v=17$. The 10 m normal incidence scanning monochromator at the beamline U125/2 of the BESSY II synchrotron, combined with a home-built target chamber and equipped with a variety of detectors, was used to unravel information on ionization, dissociation, and intramolecular fluorescence decay for the $D^{1}Π_u$ vibrational series. The combined results yield accurate information on the characteristic Beutler–Fano profiles associated with the strongly predissociated $Π_u^+$ parity components of the $D^{1}Π_u$ levels. Values for the parameters describing the predissociation width as well as the Fano-$q$ line shape parameters for the $J=1$ and $J=2$ rotational states were determined for the sequence of vibrational quantum numbers up to $v=17$. © 2010 American Institute of Physics. [doi:10.1063/1.3502471]

I. INTRODUCTION

The energy region from 110 000 to 134 000 cm$^{-1}$ in the absorption spectrum of molecular hydrogen is dense and complex, featuring a multiline spectrum. In particular, in this energy range, the electronic and vibrational energy separations become of similar magnitude, while rotational splittings remain large as well. The $D^{1}Π_u^-X^{1}Σ_g^+$ system gives rise to a well-marked sequence of intense resonances in this region. Hopfield$^1$ observed the $D^{1}Π_u$ state for the first time, but failed to find the correct sequence of vibrational levels. This was established in the early work by Beutler and co-workers$^2$ and by Richardson.$^3$ From an extrapolation of the vibrational sequence, they deduced that below the lowest predissociated level, there exist three lower vibrational levels $v=0−2$, with weaker apparent intensity. These assignments of the vibrational sequence in the $D^{1}Π_u$ state were later confirmed in subsequent higher resolution studies by Namioka,$^4$ Monfils,$^5$ Takezawa,$^6$ and Herzberg and Jungen.$^7$ A potential energy curve of the $D^{1}Π_u$ state, calculated by Dressler and Wolniewicz,$^8$ along with the other relevant potential curves of singlet-$u$ symmetry for interpreting the results of the present study, is displayed in Fig. 1.

The unpredissociated states, giving rise to sharp lines in the spectrum, have been studied to a high degree of accuracy. Analysis of classical spectrograph emission spectra by Abgrall et al.$^9$ yielded accurate level energies up to high rotational quantum numbers for both parity components of $D^{1}Π_u$ ($v=0−2$). Since the $Π^-$ parity components of the higher lying vibrational levels $v > 2$ of the $D^{1}Π_u$ state undergo only very weak predissociation,$^{10,11}$ the Q lines probing $D^{1}Π_u^-$ levels are observed as sharp. That made it possible for Abgrall et al.$^9$ to also determine the accurate line positions from emission studies for lines probing up to $v$...
= 14. Extreme ultraviolet laser-based absorption was used by Reinhold et al.\textsuperscript{12} to record high resolution spectra of the D-X(1,0) band at an even better accuracy. The most accurate level energies of the unpredissociated levels were obtained in the work combining Doppler-free laser excitation and visible and near-infrared Fourier transform emission spectroscopy\textsuperscript{13,14} yielding accuracies as good as 0.005 cm\textsuperscript{-1} for D \( \nu = 0 \)–2 levels.

Beutler\textsuperscript{2} reported on the observation of asymmetrically broadened line shapes in the R-branches of the D-X system for excited vibrational levels \( \nu > 2 \). These shapes were interpreted as Beutler–Fano profiles, resulting from an interference between a bound and a continuum state in an excitation spectrum, as first observed in the autoionization of noble gas atoms by Beutler\textsuperscript{15} and explained by Fano\textsuperscript{16,17}. The first theoretical calculations of the widths were performed\textsuperscript{18–20} in 1971 simultaneously with an experimental study by Comes and Schumpe.\textsuperscript{21} It was settled that the predissociation of the \( \Pi^+ \) parity component of the D \( ^1 \Pi_u \) state must be attributed mainly to an interaction with the B' \( ^1 \Sigma_u^+ \) continuum. A more recent calculation\textsuperscript{22} shows that the 2\( \pi \)\( \pi \)\( B' \)\( ^1 \Sigma_u^+ \) and 2\( \pi \)\( \pi \)\( C \)\( ^3 \Pi_u^\text{g} \) continua have only an effect on the ratio between H(2\( \chi \)) and H(2\( \pi \)) dissociation fragments. Mental and Gentieu\textsuperscript{23} and later Guyon et al.\textsuperscript{10} performed measurements detecting Ly-\( \alpha \) radiation emitted by the dissociation product. A pioneering study was conducted by Jungen and Atabek\textsuperscript{24} in which a full multichannel quantum defect (MQDT) treatment of the B, B', C, B'' and D systems was conducted. Level energies up to \( \nu = 13 \) were calculated for the \( \Pi^+ \) components. The \( \Lambda \)-doubling was determined for the unpredissociated bands (0,0)–(2,0) for levels \( J = 1, 3, \) and 5 as well as for the first predissociated band (3,0) for \( J = 1 \).

The issue of the asymmetry of the line shapes and the Fano-\( q \) parameters was studied in detail by Glass-Maujean et al.\textsuperscript{25} and by Dehmer and Chopka.\textsuperscript{26} In addition to absorption with classical light sources, lasers were also used to investigate the predissociation in the D \( ^1 \Pi_u \) state. The studies by Rothschild et al.\textsuperscript{27} used a laser with a superior instrument width of 0.005 cm\textsuperscript{-1} to investigate H\(_2\) at room temperature Doppler broadening exceeding 1 cm\textsuperscript{-1} to yield accurate widths and asymmetry parameters for a number of lines, mainly of hydrogen isotopomers. Croman and McCormack\textsuperscript{28} performed a two-step laser excitation investigating the \( \nu = 12 \) and 13 states of D \( ^4 \) \( \Pi_u \).

The present spectroscopic study reinvestigating the D \( ^1 \Pi_u \cdot X \Sigma_g^+ \) system in H\(_2\) is based on two different experimental approaches, both connected to a major synchrotron facility. The novel and unique Fourier transform spectrometer at the SOLEIL synchrotron facility (France) on the DESIRS vacuum ultraviolet (VUV) beamline used to record Fourier transform (FT) absorption spectra in the relevant range of 74–90 nm from a static gas sample of H\(_2\) cooled to approximately 100 K, resulting in high resolution spectra, limited by the Doppler contribution of 0.6 cm\textsuperscript{-1}, while the FT instrument resolution is 0.35 cm\textsuperscript{-1}. Apart from a determination of accurate transition frequencies for the narrow unpredissociated resonances, the asymmetrically broadened resonances have been studied at high resolution to obtain information on the Fano \( q \) parameters as well as predissociation widths \( \Gamma \) for individual lines. The 10 m normal-incidence monochromator at beamline U125/2 of the BESSY II synchrotron radiation facility in Berlin combined with a home-built target chamber for measuring photoabsorption, photoionization, and photodissociation by means of fragment fluorescence\textsuperscript{29,30} was used to compare the different decay channels upon excitation of the same D \( ^1 \Pi_u \cdot X \Sigma_g^+ \) system. The latter spectra recorded at a slightly lower resolution aided in assigning and disentangling the observed features.

II. EXPERIMENTAL SETUP

The major part of the experimental data in the present study was obtained with the vacuum ultraviolet Fourier transform spectrometer setup, connected to the DESIRS beamline at the SOLEIL synchrotron. Its principle of operation and unique capabilities for the UV and VUV range are described elsewhere.\textsuperscript{31,32} In short, a scanning wave-front division interferometer has been specifically developed in order to extend the FT spectroscopy technique toward the VUV range.\textsuperscript{31} The undulator-based DESIRS beamline provides the 7% bandwidth continuum background, which is analyzed by the FT spectrometer after it has passed an absorption cell. A typical recording of such a full spectrum recorded after passing the absorption cell is displayed in Fig. 2. Recently, the same setup was used to record high resolution spectra of narrow transitions in the Lyman and Werner bands of the hydrogen deuteride molecule in the wavelength range of 87–112 nm.\textsuperscript{33} The undulator profile covering roughly 5000 cm\textsuperscript{-1} is well approximated by a Gaussian function. The spectral range of 115 000–135 000 cm\textsuperscript{-1}, covered in the present study, was divided into four overlapping measurement windows.

The H\(_2\) spectra are recorded under quasistatic conditions. Hydrogen gas passes through a needle valve regulator into a T-shaped, windowless free flow cell of 100 mm length and 12 mm inside diameter. This results in an inhomogeneous density distribution along the path of the synchrotron radiation, for which an integrated column density can only be
estimated. It is set by regulating the pressure just outside the
target cell for appropriate absorption conditions, i.e., the
unity optical depth for the main features under investigation.
Spectra were recorded at three different settings of the pressure
at the inlet needle valve.

Once the radiation has passed through the target cell, it
takes the spectrometer and an interferogram is generated.
For the present study, recordings are taken at 512 ks, which
is the number of sampling points taken along the path of the
moving arm in the interferometer traveling over ~9 mm. A
typical measurement window in the present study took
roughly 2 h for accumulating signal over 100 interferograms.
The setting of 512 ks sampling recording corresponds to a
spectral resolution of 0.35 cm⁻¹ or a resolving power of
350 000.

The target cell was enveloped by a second cell in which
liquid nitrogen is allowed to flow, cooling the cell down to
roughly 100 K. This was done for two reasons. At lower
temperatures, the complexity of the spectrum and the overlap
of resonances are reduced; only the lowest rotational states
up to J = 2 were found to be populated. At this temperature,
the Doppler width of the H₂ lines reduces to 0.6 cm⁻¹. With
the chosen setting of the resolving power of the FT spectrometer,
this yields the narrowest width for the unpredissociated
lines at ~0.7 cm⁻¹.

An advantage of a FT spectrometer is that the wave-
length is intrinsically calibrated when the travel distance in
the moving arm is known; this is done by referencing the travel
against the fringes of a frequency stabilized HeNe laser.³¹
Additional calibration of the frequency scale is ac-
complished by calibration against the Ar line (3p)⁵(⁵P)⁹d(3/2) → (3p)⁹(⁴S)⁰ known to an accuracy of
0.03 cm⁻¹.

The spectra recorded at the BESSY II synchrotron in
Berlin were measured with a 10 m normal incidence mono-
chromator equipped with a 1200 lines/mm grating with a
spectral resolution of 2 cm⁻¹ or 0.0012 nm.³² The absorption
cell is a 39 mm long differentially pumped cell containing
27 µbar of H₂. A photodiode at the back of the cell allows
for detecting direct absorption at room temperature. An elec-
trode in the target cell attracts photoinions, and the Ly-α flu-
oscence is measured with a microchannel plate detector.
Molecular fluorescence is recorded via a detector sensitive to
visible radiation. All the signals mentioned above were re-
corded as a function of incident photon energy so that reli-
able comparisons can be made and relate the cross sections
of the various decay channels. This experimental setup
allows absolute intensity measurements and quantitative
dynamical studies.

III. PREDISSOCIATION IN THE D ¹Πᵤ STATE

It was already understood at an early stage that the pre-
dissociation of the 3pν D ¹Πᵤ state proceeds via coupling to
the continuum of the 3pν B' ¹Σᵤ⁺ state.³³ ³⁴ There is no cou-
pling between the states of u and g inversion symmetry; thus,
there are three candidates with the same u symmetry for the
D state predissociation mechanism: the 2pπC ¹Πᵤ, 2pσB ¹Σᵤ⁺, and 3pνB' ¹Σᵤ⁺ states. The Coriolis coupling to the
B' state is the chief cause of the predissociation. Coupling to
the C state is two orders of magnitude weaker and coupling to the B state is even smaller by at least one order of magnitude.³⁶ The B' and D states approach the same elec-
tronic He(3p) configuration in the united atom limit so the
Coriolis coupling may be very effective. The same interac-
tion between D and B' states responsible for predissociation
causes severe level shifts:³⁵ the Λ-doubling splitting even in
the bound region below the n = 2 dissociation limit. Predi-
sociation of the D ¹Πᵤ state results in H(n = 2) excited atomic fragments.³⁶ In the case of the production of H(2p), the
dissociation product can be observed via Lyman-α fluorescence and the H(2s) atoms are observed in most cases via the
same fluorescence due to collisions to the H(2p) state.

The physics of a bound state interacting with a con-
tinuum state, where both states are simultaneously excited
from a ground level, was described by Fano.¹⁷ If there is
oscillator strength in both channels, such interference leads
to asymmetric line shape, also referred to as a Beutler–
Fano line shape, which is described by a q-parameter, indi-
cating the degree of asymmetry

\[
q = \frac{\left\langle \phi_{D_w} \right| T_{DX}(R) \left| \phi_{X_u} \right\rangle}{\pi V(\phi_{B'_w} \left| T_{B'_X}(R) \right| \phi_{X_u})}.
\]

In this formula, the nominator stands for the transition dipole
matrix element [T(R) being the R-dependent transition dipole
moment] for excitation from the ground state X ¹Σ_g⁻ to the
excited state, which is in the present case a certain rovi-
brational level in the D ¹Π_u state.³⁷ The denominator contains
the matrix element for excitation to the continuum channel,
which is in the present specific case represented by the
B' ¹Σ_u⁺ state. V represents the interaction matrix element be-
tween the two excited channels, the discrete and the con-
tinuum, with, in this case, the D and B' states signifying the
coupling of the bound state with the continuum. The matrix
element for the rotational coupling operator, H, yields for the
interaction matrix element³⁸

\[
V = \left\langle \phi_{B'_w} \right| H \left| \phi_{D_w} \right\rangle \propto \sqrt{J(J+1)}.
\]

Hence, the Fano q parameter is inversely proportional to ro-
tation. The predissociation widths Γ are related to the square
of the interaction matrix element
\[ \Gamma = 2\pi v^2. \] 

also exhibiting a rotational dependence proportional to \(J(J+1)\).

Various theoretical calculations of the widths of the \(\Pi^+\) parity components of the \(D^1\Pi_u\) states surfaced in the early 1970s by Julienne\(^{18}\) and Fiquet-Fayard and Gallais,\(^{19}\) showing that the predissociation in the \(D^1\Pi_u\) state must indeed be attributed to an interaction with the \(B^1\Sigma_u^+\) continuum. Initially, the two calculations were in disagreement with one another until a missing factor of 4 was discovered in the calculation by Julienne.\(^{20}\) The two theoretical studies were still in disagreement with the measured values of Comes and Shumpe\(^{21}\) by roughly 25%. The experimental widths varied in a way not predicted by theory. Further measurements using the \(J\) dependence of \(q, \Gamma\), and the intensities by Glass-Maujean \(^{22}\) et al. gave a far better agreement with Julienne's\(^{18}\) and Fiquet-Fayard and Gallais's\(^{19}\) values for \(v = 3 – 5\) but still disagreed by roughly 25% for \(v = 7 – 11\).

The accuracy of the theoretical modeling of the predissociative widths is determined mainly by the accuracy of the potential curves used. The coupling to the \(B\) and \(C\) states does not have an effect on the predissociative widths but does play a role in the \(H(2s)/(H(2s)+H(2p))\) branching ratio. The coupling to the \(B\) state was included in the calculations by Borondo \(^{23}\) et al. in their calculation of the branching ratio. Beswick and Glass-Maujean\(^{24}\) conducted further studies on this topic, including the predissociation of the \(D\) state. Line shapes were obtained from solving the appropriate coupled Schrödinger equation, yielding values for the predissociative widths and \(q\)-parameters. In a study by Mrugala,\(^{20}\) the shifts between \(\Pi^-\) and \(\Pi^+\) levels were calculated. Mrugala\(^{25}\) benefited from the accurate \textit{ab initio} calculations of the \(D\)-\(B^1\Sigma_u^+, D-B, D-C,\) and \(D-D^1\) couplings together with improved potential energy curves for the \(B, B', C, D,\) and \(D'\) states. All nonadiabatic interactions between the \(D, B,\) and \(B'\) state were included within the close-coupling approach.

A multichannel quantum defect approach was followed by Gao \(^{26}\) et al. In the framework used, the interactions between the \(D, B',\) and \(C\) states were included in a noniterative eigenchannel R-matrix approach. The effect of ionization was thought to be small in comparison to predissociation and was not included in the calculation. Furthermore, the \(B\) state interaction was neglected because of weak coupling to the \(D\) state. The calculation yields widths for the \(J = 2\) level of the \(D\) state that closely match the experimental values observed by Glass-Maujean and co-workers.\(^{22}\)

The \(\Pi^-\) parity components of the \(3p\pi D^1\Pi_u\) state, probed in Q-transitions, undergo only very weak predissociation, for which coupling to the lower lying \(2p\pi C^1\Pi_u\) is the only symmetry-allowed possibility. The effect of this homogeneous perturbation in terms of predissociation widths of the \(Q(1)\) transitions was calculated by Glass-Maujean \(^{26}\) et al.\(^{30}\) An MQDT analysis produced line positions and intensities for the \(Q(J) (J = 1 – 4)\) absorption transitions.\(^{12}\) In MQDT calculations, all the interactions of the \(np\pi^1\Pi_u^+\) states were included and not only the \(C\) and \(D'\) states. The results of these calculations were consistent with the observations of Lyman-\(\alpha\) fluorescence and visible molecular fluorescence.\(^{30,42}\)

### IV. EXPERIMENTAL RESULTS AND DISCUSSION

The vacuum ultraviolet Fourier transform spectra show the features of the \(D^1\Pi_u-X^1\Sigma_u^+(v, 0)\) bands for \(\text{H}_2\) up to \(v = 17\), which is the uppermost bound vibrational level in this potential. Figure 3 displays the detail recordings of some of the regions with pronounced \(D-X\) features. In order to retrieve these spectra, the bell-shaped background continuum of the undulator profiles, as shown in Fig. 2, was transformed into a flat continuum by fitting the background with a Gaussian function. The measurement window was divided through by the Gaussian fit resulting in a flat background. In a second step, the Beer–Lambert absorption depth was linearized, and the scale inverted to arrive at the spectra depicted in Fig. 3. The spectrum in Fig. 3(a) shows the unpredissociated \(D-X(0,0)\) band; hence, these lines represent the limiting resolution of the spectral method. The widths of \(\sim 0.7\ \text{cm}^{-1}\) are
a result of Doppler broadening (0.6 cm$^{-1}$ for H$_2$ at 100 K) and the instrumental width of 0.35 cm$^{-1}$ from the settings of the FT instrument.

The uncertainties in the line positions are governed by the signal to noise ratio, the width of the transition, and the number of points that the transition consists of. When all systematic effects of the FT spectrometer are taken into account, the accuracy is limited to 0.03 cm$^{-1}$. The so-called $p$ parameter, connected to an interferometric setup with a HeNe reference laser controlling the path length travel, is adjusted depending on the operational wavelength regime. It was discovered that the changing of this parameter induces small systematic effects on the wavelength calibration. In the present study, these effects were not accounted for and so, a conservative estimate of the statistical deviation in the line positions for the unpredissociated lines ($v=0–2$) and the $\Pi^-$ components is 0.06 cm$^{-1}$. For the broad $\Pi^+$ components, the uncertainty is in the range of 0.3 cm$^{-1}$, while for the blended bands (7,0), (8,0), and (9,0), the uncertainty increases to 0.6 cm$^{-1}$.

**A. Spectroscopy**

The transition energies resulting from the combined set of spectra are listed in Table I. The corresponding level energies are available via the supplementary material data depository of the American Institute of Physics. Various line shape fitting methods were employed to derive the line positions; for the asymmetric Fano line shapes, the true transition frequency was derived from the deconvolution procedure explained in Sec. IV C.

The assignment of the unpredissociated lines derives straightforwardly from the accurate emission data, while for higher lying levels for the $D$ $1\Pi^+$ components, the multichannel quantum defect calculations are a guidance. For the transitions to the $1\Pi^+$ components of $v=14–17$, that information is lacking. These levels were identified starting with the $2\Pi^+$ components and setting the A-doubling to zero. Where lines appear to be blended, the assignments and analysis were aided by the dissociation spectra. In particular, the R(1) line of the (14,0) band was obscured by a particularly strong, unidentified transition. As shown in Fig. 4, this feature could not have been assigned properly without the aid of the dissociation spectrum.

Other lines analyzed in the dissociation spectrum are the R(0) and R(1) lines in the (16,0) band and the R(1) line in the (17,0) band. These transitions were rather weak in the FT absorption spectrum but appeared clearly in the dissociation spectrum. Due to the lower resolution of the spectrometer at BESSY and to the higher temperature of the gas, the uncertainty in the position for these measurements is slightly better than 1 cm$^{-1}$.

Several additional problems determining accurate line positions and line parameters occurred. The R(1) transition in the $D-X(6,0)$ band is blended by a transition to the $B^\prime$ state. This presents a complication in that the lines are blended in both the absorption and dissociation spectra since both states predissociate. In this case, the blending with the R(0) transition in the $B^\prime-X(4,0)$ band is such that no data could be extracted. Similarly the R(1) transition in the $D-X(7,0)$ band is blended by the R(1) transition in the $B^\prime-X(5,0)$ band and by the Q(1) transition of the $D^\prime-X(4,0)$ band; no data on the predissociated widths could be extracted. The positions specified in Table I are those from the deconvoluted fit. Due to the relatively small shift of the line position (from the interaction with the continuum), we believe that the fit does provide the true line center. The R(0) transition of the (7,0) band is blended by a R(0) transition from the $5\sigma_r v=3$ Rydberg series; the position and the widths were determined by deconvolving with the overlapping line. The R(0) transition in the (8,0) band is blended with an R(0) transition from the $6\sigma_r (v=3)$ Rydberg series. Again, a fit was achieved from which an overlapping line was deconvolved, this is shown in Fig. 3(d). The (9,0) band was superimposed upon three different Rydberg series (17$\pi\pi$ $v=2$, 22$\sigma_r$ $v=2$, and 7$\pi\pi$ $v=3$); line positions and widths for R(0) and R(1) were determined by deconvolution.

The transitions of the first three unpredissociated bands $v=0–2$ were compared to the measurements of Bailly et al., which are accurate to 0.005 cm$^{-1}$ for the $D$ system. The comparison is good with an average deviation of −0.03 cm$^{-1}$, thus demonstrating the high absolute accuracy of the FT instrument. The fitted positions of the $\Pi^-$ states were compared with the measurements of Abgrall et al. for $v=3–14$, which we consider to be accurate to within 0.1 cm$^{-1}$. The overall agreement between these Q lines is better than 0.1 cm$^{-1}$ except for $v=14$.

We compare to the measurements of Glass-Maujean et al. for the $\Pi^-$ components probing Q(1) transitions for $v=15–17$ in Table I. There appears to be a discrepancy between our measurements and those compiled by Glass-Maujean et al. for the last three bands, (15,0) (16,0), and (17,0); yet, this is still within the experimental uncertainty of 6 cm$^{-1}$ for that specific experimental configuration. In a later publication, these measurements were compared to a MQDT calculation. Discrepancies in the order of 5 cm$^{-1}$ were found for these three bands once again within the experimental uncertainty. The present measurements side with the MQDT calculations and the comparison can be found in Table I. The comparison is suggestive of an accuracy better than 1 cm$^{-1}$, thus confirming the high accuracy of these calculations.

For the $\Pi^+$ components, the present measurements were compared to those of Takezawa for $v=3–11$. Deviations amount to several 0.1 cm$^{-1}$ due to the lower accuracy in the classical absorption study, where no Fano analysis was conducted and no pressure corrections were made. One exception was the R(0) transition in the (7,0) band where a deviation of more than 11 cm$^{-1}$ was found; we attribute this to either a misassignment or a typo and therefore compare to the data of Herzberg and Junger. Lines in bands (12,0) and (13,0) were compared to the measurements of Coman and McCormack. The discrepancies of the order of cm$^{-1}$ indicate that these laser-based data were not calibrated on an absolute scale.
TABLE I. Transition energies in cm$^{-1}$ and predissociated linewidths $\Gamma$ in cm$^{-1}$ for the measured transitions in the $D$ $^1\Pi_u$ $^1\Sigma_u^+$ $(v, 0)$ system of H$_2$. The widths measured for the unpredissociated levels $v=0$−2 and the Q(1) transitions are limited by the Doppler broadening and therefore not specified in the table. $\Delta$ represents deviations between the present values minus the previously published data. For excited states $v=0$−2, comparison was made with Bailly et al. (Ref. 14). For the $\Pi^+$ components in $v=3$−11, comparison was made with Takezawa (Ref. 6). For $v=12$ and 13, we compare to Croman and McCormack (Ref. 28), and for the remaining bands, the measurements of SOLEIL were compared to those from BESSY. The $\Pi^−$ components of $v=3$−14 are compared with the measurements of Abgrall et al. (Ref. 10), 14 are compared with the measurements of Abgrall et al. (Ref. 10), and for $v=15$−17, we compare to Glass-Maujean et al. (Ref. 29). $\Delta_M$ represents a comparison with the MQDT calculations of Glass-Maujean and Jungen (Ref. 42); these calculations are available for the Q(1) transitions only.

<table>
<thead>
<tr>
<th>Transition</th>
<th>Energy</th>
<th>$\Delta$</th>
<th>$\Gamma$</th>
<th>$\Delta_M$</th>
</tr>
</thead>
<tbody>
<tr>
<td>D-X(0,0)</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Q(1)</td>
<td>112 813.14</td>
<td>−0.03</td>
<td>⋯</td>
<td>−0.39</td>
</tr>
<tr>
<td>R(0)</td>
<td>112 935.25</td>
<td>−0.03</td>
<td>⋯</td>
<td>⋯</td>
</tr>
<tr>
<td>R(1)</td>
<td>112 941.20</td>
<td>0.03</td>
<td>⋯</td>
<td>⋯</td>
</tr>
<tr>
<td>D-X(1,0)</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Q(1)</td>
<td>115 035.88</td>
<td>−0.04</td>
<td>⋯</td>
<td>−0.54</td>
</tr>
<tr>
<td>R(0)</td>
<td>115 155.80</td>
<td>−0.01</td>
<td>⋯</td>
<td>⋯</td>
</tr>
<tr>
<td>R(1)</td>
<td>115 151.14</td>
<td>−0.02</td>
<td>⋯</td>
<td>⋯</td>
</tr>
<tr>
<td>D-X(2,0)</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Q(1)</td>
<td>117 129.34</td>
<td>−0.04</td>
<td>⋯</td>
<td>−0.67</td>
</tr>
<tr>
<td>R(0)</td>
<td>117 251.64</td>
<td>−0.07</td>
<td>⋯</td>
<td>⋯</td>
</tr>
<tr>
<td>R(1)</td>
<td>117 244.82</td>
<td>−0.02</td>
<td>⋯</td>
<td>⋯</td>
</tr>
<tr>
<td>D-X(3,0)</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Q(1)$^a$</td>
<td>119 097.37</td>
<td>0.02</td>
<td>⋯</td>
<td>−0.65</td>
</tr>
<tr>
<td>R(0)</td>
<td>119 217.99</td>
<td>0.39</td>
<td>4.94</td>
<td>⋯</td>
</tr>
<tr>
<td>R(1)</td>
<td>119 203.60</td>
<td>1.6</td>
<td>13.72</td>
<td>⋯</td>
</tr>
<tr>
<td>D-X(4,0)</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Q(1)$^b$</td>
<td>120 942.76</td>
<td>0.05</td>
<td>⋯</td>
<td>−0.7</td>
</tr>
<tr>
<td>R(0)</td>
<td>121 063.05</td>
<td>0.65</td>
<td>4.40</td>
<td>⋯</td>
</tr>
<tr>
<td>R(1)</td>
<td>121 042.48</td>
<td>0.48</td>
<td>14.22</td>
<td>⋯</td>
</tr>
<tr>
<td>D-X(5,0)</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Q(1)$^b$</td>
<td>122 667.75</td>
<td>0.06</td>
<td>⋯</td>
<td>−0.76</td>
</tr>
<tr>
<td>R(0)</td>
<td>122 787.94</td>
<td>0.54</td>
<td>4.25</td>
<td>⋯</td>
</tr>
<tr>
<td>R(1)</td>
<td>122 760.86</td>
<td>0.16</td>
<td>14.30</td>
<td>⋯</td>
</tr>
<tr>
<td>D-X(6,0)</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Q(1)</td>
<td>124 273.90</td>
<td>0.03</td>
<td>⋯</td>
<td>−0.71</td>
</tr>
<tr>
<td>R(0)</td>
<td>124 393.75</td>
<td>0.15</td>
<td>3.58</td>
<td>⋯</td>
</tr>
<tr>
<td>R(1)$^b$</td>
<td>⋯</td>
<td>⋯</td>
<td>⋯</td>
<td>⋯</td>
</tr>
<tr>
<td>D-X(7,0)</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Q(1)$^b$</td>
<td>125 759.85</td>
<td>0.03</td>
<td>⋯</td>
<td>−0.59</td>
</tr>
<tr>
<td>R(0)$^{a,c}$</td>
<td>125 877.03</td>
<td>0.43</td>
<td>3.60</td>
<td>⋯</td>
</tr>
<tr>
<td>R(1)$^b$</td>
<td>125 841.35</td>
<td>0.55</td>
<td>⋯</td>
<td>⋯</td>
</tr>
<tr>
<td>D-X(8,0)</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Q(1)</td>
<td>127 129.23</td>
<td>0.09</td>
<td>⋯</td>
<td>−0.57</td>
</tr>
<tr>
<td>R(0)$^b$</td>
<td>127 246.84</td>
<td>−1.66</td>
<td>3.42</td>
<td>⋯</td>
</tr>
<tr>
<td>R(1)</td>
<td>127 201.15</td>
<td>−1.35</td>
<td>11.65</td>
<td>⋯</td>
</tr>
<tr>
<td>D-X(9,0)</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Q(1)</td>
<td>128 377.38</td>
<td>−0.07</td>
<td>⋯</td>
<td>−0.44</td>
</tr>
<tr>
<td>R(0)$^b$</td>
<td>128 496.54</td>
<td>0.34</td>
<td>3.71</td>
<td>⋯</td>
</tr>
<tr>
<td>R(1)$^b$</td>
<td>128 444.94</td>
<td>0.04</td>
<td>9.17</td>
<td>⋯</td>
</tr>
<tr>
<td>D-X(10,0)</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Q(1)</td>
<td>129 502.50</td>
<td>0.13</td>
<td>⋯</td>
<td>−0.21</td>
</tr>
</tbody>
</table>
B. Λ-doubling

In Fig. 5, the splitting between different Π* and Π− parity levels for the J=1 level has been plotted as detected from the current measurements. This involves adding the ground state energy difference between rotational levels J=0 and 1 to the Q(1) transitions and subtracting this from the R(0) transitions (the ground state rotational energy splitting of 118.486 cm⁻¹ was taken from the accurate calculations of Wolniewicz⁴⁶). Values for this Λ-doubling have been plotted for each vibration up to v=17. The two “accidents,” v=13 and v=17, could be due to local couplings.

The lowest three bound states of the D system are subject to strong perturbations from the last few bound levels of the B' system.⁴⁵ This explains the "accidental" behavior seen for the Λ-doubling in v=1 and 2 in Fig. 5 and the reversal between the R(0) and R(1) lines in Fig. 3(a). The Λ-doubling turns into a smooth decaying function from v ≥ 3 toward high v. We postulate that the Λ-doubling is due to the interaction between the discrete D states and the summed contribution of low-lying discrete levels in the B' state and the B' continuum. Hence, the physical origin of the Λ-doubling is connected to that of the origin of the predissociation of the D-state (discussed below). Both phenomena become weaker toward high vibrational levels due to reduced vibrational wave function overlap between the D and B' levels. The present data shows excellent agreement with calculations for the Λ-doubling for vibrational levels⁴⁴,⁴⁰ v =0–6.

C. Predissociation analysis

Initially, a two component fit of the data in q and Γ was made with a Fano function. The contribution of the instru-

---

**TABLE I. (Continued.)**

<table>
<thead>
<tr>
<th>Transition</th>
<th>Energy</th>
<th>Δ</th>
<th>Γ'</th>
<th>Δ&quot;</th>
</tr>
</thead>
<tbody>
<tr>
<td>R(0)</td>
<td>129 621.43</td>
<td>−0.07</td>
<td>3.61</td>
<td>⋯</td>
</tr>
<tr>
<td>R(1)</td>
<td>129 563.49</td>
<td>0.79</td>
<td>9.27</td>
<td>⋯</td>
</tr>
<tr>
<td>D-X(11,0)</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Q(1)</td>
<td>130 499.61</td>
<td>0.09</td>
<td>⋯</td>
<td>0.05</td>
</tr>
<tr>
<td>R(0)</td>
<td>130 618.52</td>
<td>−3.18</td>
<td>3.85</td>
<td>⋯</td>
</tr>
<tr>
<td>R(1)</td>
<td>130 554.15</td>
<td>−0.45</td>
<td>10.27</td>
<td>⋯</td>
</tr>
<tr>
<td>D-X(12,0)</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Q(1)</td>
<td>131 366.00</td>
<td>0.10</td>
<td>⋯</td>
<td>0.21</td>
</tr>
<tr>
<td>R(0)</td>
<td>131 484.50</td>
<td>−0.77</td>
<td>1.93</td>
<td>⋯</td>
</tr>
<tr>
<td>R(1)</td>
<td>131 414.00</td>
<td>−0.76</td>
<td>9.67</td>
<td>⋯</td>
</tr>
<tr>
<td>D-X(13,0)</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Q(1)</td>
<td>132 093.33</td>
<td>−0.11</td>
<td>⋯</td>
<td>−0.29</td>
</tr>
<tr>
<td>R(0)</td>
<td>132 212.33</td>
<td>1.96</td>
<td>2.44</td>
<td>⋯</td>
</tr>
<tr>
<td>R(1)</td>
<td>132 134.47</td>
<td>−2.04</td>
<td>4.09</td>
<td>⋯</td>
</tr>
<tr>
<td>D-X(14,0)</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Q(1)</td>
<td>132 673.74</td>
<td>0.49</td>
<td>⋯</td>
<td>−0.67</td>
</tr>
<tr>
<td>R(0)</td>
<td>132 792.37</td>
<td>−0.76</td>
<td>2.15</td>
<td>⋯</td>
</tr>
<tr>
<td>R(1)</td>
<td>132 706.89</td>
<td>⋯</td>
<td>4.82</td>
<td>⋯</td>
</tr>
<tr>
<td>D-X(15,0)</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Q(1)</td>
<td>133 100.81</td>
<td>−7.13</td>
<td>⋯</td>
<td>−0.78</td>
</tr>
<tr>
<td>R(0)</td>
<td>133 219.34</td>
<td>0.49</td>
<td>1.12</td>
<td>⋯</td>
</tr>
<tr>
<td>R(1)</td>
<td>133 124.96</td>
<td>0.17</td>
<td>3.30</td>
<td>⋯</td>
</tr>
<tr>
<td>D-X(16,0)</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Q(1)</td>
<td>133 366.45</td>
<td>−6.01</td>
<td>⋯</td>
<td>−0.67</td>
</tr>
<tr>
<td>R(0)d</td>
<td>133 484.59</td>
<td>⋯</td>
<td>2.33</td>
<td>⋯</td>
</tr>
<tr>
<td>R(1)d</td>
<td>133 381.11</td>
<td>⋯</td>
<td>2.51</td>
<td>⋯</td>
</tr>
<tr>
<td>D-X(17,0)</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Q(1)</td>
<td>133 468.31</td>
<td>−5.44</td>
<td>⋯</td>
<td>0.17</td>
</tr>
<tr>
<td>R(0)</td>
<td>133 587.77</td>
<td>−0.27</td>
<td>0.38</td>
<td>⋯</td>
</tr>
<tr>
<td>R(1)</td>
<td>133 472.62</td>
<td>⋯</td>
<td>1.35</td>
<td>⋯</td>
</tr>
</tbody>
</table>

aSlightly saturated.
bBlended in the absorption spectra.
cCompared with the data of Herzberg and Jungen (Ref. 7).
dData from dissociation spectra.
The $D-X(14,0)$ band of H$_2$ displays the R(0), R(1), and Q(1) lines recorded by various methods. (a) The high resolution absorption spectrum recorded with the Fourier transform setup at SOLEIL. (b) The absorption spectrum recorded with the 10 m normal incidence scanning monochromator at room temperature. (c) The photoionization spectrum. (d) The spectrum recorded by detection of Lyman-$\alpha$ photons originating from the dissociation fragments. (e) The fluorescence from the H$_2$ D state decaying to high-lying levels of $g$ symmetry in the molecule, with cascades from these $g$ states to the $B$ state (Ref. 11). Note that the intensities in spectra (b)–(d) represent absolute cross sections. Spectra (b)–(e) were obtained at BESSY.

The extracted $q$ parameters for the R(1) transitions are shown in Fig. 6. The determination of the $q$ parameter is complicated due to two reasons: first, the noise on the spectrum, and second, imparting a resolution condition on two superimposed Fano functions. In Fig. 7, this is illustrated for the specific case of the $D-X(3,0)$ band, where a rather accurate value of $q=-5.90\pm0.55$ is derived in a two component fit optimizing for $q$ and $\Gamma$. In the figure, we compare the two component fit to a one component fit of $\Gamma$ only. The fit is insensitive to a variation in $q$, while there is very little correlation between the two parameters. This is most clear for the R(0) transition where the $q$ parameter has doubled yet the width changes by just over 0.1 cm$^{-1}$. Due to the broad, asymmetric nature, it is difficult to address how far these lines are resolved. This may lead to an erroneous determination of the $q$ parameter. To compare this to the ideal case, the R(1) transition for $v=10$ is clearly resolved with good signal to noise ratio [see Fig. 3(e)]. The resulting $q$ parameter determined is $-8.50\pm0.08$, which compares well to the calculated value expected to be close to $-9$. In order to obtain the $\Gamma$ parameters specified in Table I, the $q$ parameters were fixed for the R(0) and R(1) transitions to the calculated $v$ dependent values [35] for $v=3$–5. For the remaining vibrations, $v=8$–17 values of $-19.55$ for R(0) transitions and $-9.3$ for the R(1) transitions were used [40].

The results for the widths of the $J=1$ levels are displayed in Fig. 8. To our knowledge, there is no MQDT calculation for $J=1$ levels and the measured values are lacking.

FIG. 4. The $D-X(14,0)$ band of H$_2$ displaying the R(0), R(1), and Q(1) lines recorded by various methods. (a) The high resolution absorption spectrum recorded with the Fourier transform setup at SOLEIL. (b) The absorption spectrum recorded with the 10 m normal incidence scanning monochromator at room temperature. (c) The photoionization spectrum. (d) The spectrum recorded by detection of Lyman-$\alpha$ photons originating from the dissociation fragments. (e) The fluorescence from the H$_2$ D state decaying to high-lying levels of $g$ symmetry in the molecule, with cascades from these $g$ states to the $B$ state (Ref. 11). Note that the intensities in spectra (b)–(d) represent absolute cross sections. Spectra (b)–(e) were obtained at BESSY.

FIG. 5. Values of the $\Lambda$ doubling for the $D^1\Pi_J=1$ levels as a function of vibrational quantum number. The sign is such that $\Pi^\ast$ or $\Pi_{1/2}$ levels are higher than $\Pi^-$ or $\Pi_{3/2}$ levels. The values of the $\Lambda$ doubling for $\nu=7$ and 8 have been omitted due to blending of the R(0) and Q(1) transitions.

FIG. 6. The fitted $q$ parameters for the R(1) transitions compared with the measured values of Glass-Maujean et al. (Ref. 25) and the calculated values of Beswick and Glass-Maujean (Ref. 22) and Mrugala (Ref. 40). Overlapping values have been slightly offset along the x-axis to make the error bars clearly visible.

FIG. 7. FT spectrum of the $D-X(3,0)$ band of H$_2$ with a comparison between the two component fits of $q$ and $\Gamma$ and a one component fit of $\Gamma$ only. The resulting values of the parameters for the two component fits were $q=-5.90\pm0.55$ and $\Gamma=12.7\pm1.1$ cm$^{-1}$ for R(1), and $q=-43\pm35$ and $\Gamma=5.10\pm0.26$ cm$^{-1}$ for R(0). In a one component fit, fixing $q$ parameters to those obtained by theory (Ref. 40) yields $\Gamma=13.6\pm1.0$ cm$^{-1}$ for R(1) and $\Gamma=4.97\pm0.26$ cm$^{-1}$ for R(0).
The superior resolution of the novel VUV Fourier transform instrument is applied for a reinvestigation of the D-X absorption system in H₂. This system is a benchmark system for the study of predissociation in diatomic molecules with the special feature of pronounced Fano-type line shapes. In H₂, the smallest neutral molecular system, the widths and $\eta$-asymmetry parameters can be calculated in various first principles schemes to be compared at a high level of accuracy to experiment. The presently measured transition frequencies are the most accurate and signify an order of magnitude improvement in accuracy over previous studies.\(^5,6,21\)

The data are extended up to the highest $v=17$ vibrational level in the $D^1Π_u$ state. The FT spectrometer has a far better resolution than that obtained by scanning monochromators, but with the measurement limited to direct absorption only, it cannot provide all the information of the interaction between light and molecules. In this way, the combination of the two experimental techniques, the FT absorption spectrum from SOLEIL and the scanning monochromator measurements from BESSYII, are complementary. This leads to an almost complete characterization of the molecular state.

The extracted predissociation widths are found to decrease up to $v=10$ as expected from theory, with indication of a possible sudden increase in $\Gamma$ at $v=11$, which may be explained by the opening up of an additional predissociation channel associated with the $B'^1Π$ double well state. The smooth development of a decreasing $\Lambda$-doubling in the $D^1Π_u$ state toward higher vibrational levels is consistent with the decrease in the predissociation rates and in excellent agreement with calculation\(^24,40\) for $v=0–6$; both phenomena have their origin in overlap with the $B^1Σ_u^+$ state. The positions of the $D^1Π_u$ levels are measured to an accuracy of 0.06 cm\(^{-1}\), which is the most accurate to date. These data compare extremely well to previously calculated positions within the MQDT framework,\(^12\) suggesting an accuracy better than 1 cm\(^{-1}\) and providing further proof for its suitability for the modeling of such complex molecular processes at very high excitation energy in the molecule.

**ACKNOWLEDGMENTS**

The staff of SOLEIL and its DESIRS beamline is thanked for the support and for providing the opportunity to conduct measurements in the campaigns in 2009. This work was supported by the Netherlands Foundation for Fundamental Research of Matter (FOM). We are indebted to EU for its financial support via the Transnational Access funding scheme. M.G.M. acknowledges help from P. Reiss, H. Schmoranzer, and the BESSY staff, and is indebted to EU for

---

**FIG. 8.** The deduced values of the predissociated widths $\Gamma$ for the $J=1$ level compared with other measured and calculated values currently available in the literature. The calculations of Julienne (Ref. 18) have been multiplied by a factor of 4 to correct for an error as specified by Fiquet-Fayard and Gallais (Ref. 20).

**FIG. 9.** The deduced values of the predissociated widths $\Gamma$ for the $J=2$ level compared with other measured and calculated values currently available in literature. Overlapping values have been slightly offset along the x-axis to make the error bars clearly visible.
the support (Grant ELISA No. 226716). W.-Ü.L.T.B. is indebted to the French ANR project SUMOSTAI for the support.

44 See supplementary material at http://dx.doi.org/10.1063/1.3502471 for the measured level energies of the $D^4\Pi_u$ system of $H_2$. Levels with positive and negative total parity for $J=1$ are listed, while for $J=2$ only the levels with positive total parity are listed.